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Primordial Nucleosynthesis

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- □ Introduction to Standard Big-Bang Nucleosynthesis
- □ ⁴He, D, ³He, ⁷Li observations
- Nuclear reactions
- Concordance observations/SBBN
- Physics of Standard BB
- Examples of non-Standard BBN
- Conclusions

Three observational evidences for the Big-Bang Model

1. The expansion of the Universe

Galaxies move away from each other according to Hubble's law: $V = H_0 \times D$ with $H_0 \approx 72$ km/s/Mpc, the Hubble parameter (or "constant"). $D \propto a(t)$ (length scale parameter)

2. The Cosmic Microwave Background radiation (CMB)

A black body radiation at 2.7 K corresponding to the redshifted spectrum emitted when the universe became transparent

3. Primordial nucleosynthesis

Reproduces the light-elements primordial abundances over a range of nine orders of magnitudes.



 $V = H_0 \times D, H_0 \approx 72 \text{ km/s/Mpc}, h \equiv H_0/(100 \text{ km/s/Mpc})$

Where V is the recession velocity of a galaxy at a distance D



Hubble's law:
$$V = H_0 \times D$$

Direct consequence of the expansion of the Universe

Mean distance between galaxies $\propto a(t)$ [scale factor]:

$$D(t) = \chi \times a(t)$$
$$D$$
$$V = \dot{D}(t) = \chi \times \dot{a}(t) = \chi \times \dot{a}(t) / a(t)$$

$$H(t) \equiv \dot{a}(t) / a(t)$$



Redshifted spectrum of the photons released when the universe became transparent (electrons and nuclei recombination into neutral atoms)

Opacity caused by Compton scattering of photons on free electrons

As long as photoionization $H+\gamma \leftrightarrow p+e$ - is effective i.e. until $\approx 300,000$ years after the Big-Bang when T dropped to ≈ 3000 K

 $T = 3000 \text{ K} \rightarrow 2.7 \text{ K}$



 $T = 3000 \text{ K} \rightarrow 2.7 \text{ K}$

 λ (present) = λ (recombination) × *a*(present) / *a*(recombination)



 $\lambda_{emitted} = \lambda$ as measured in laboratory

0=present value

Temperature of photons-electrons decoupling

$$n_{e} = n_{p} \text{ (neutrality)}$$

$$n_{b} = n_{p} + n_{H}$$

$$Saha \text{ equation :}$$

$$\frac{X_{e}^{2}}{1 - X_{e}} = \left(\frac{m_{e}c^{2}k_{B}T}{2\pi(\hbar c)^{2}}\right)^{3/2} \frac{e^{-E_{1}/k_{B}T}}{n_{b}}$$

$$T = 2.725 \times (1+z) \text{ K}$$

$$n_{b} \approx \Omega_{b}h^{2} \times 10^{-5} \times (1+z)^{3} \text{ baryon / cm}^{3}$$

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Determination of the baryonic density of the Universe

Standard Big Bang Nucleosynthesis

Calculated and observed ⁴He, D, ³He, ⁷Li primordial abundances $\Rightarrow \eta \text{ (or } \Omega_B h^2)$ Need good:

Good.
 ➢Observational data
 ➢Nuclear data

□ HI and HeII Lyman- α forest absorption (on the line of sight of quasars)

Anisotropies in the Cosmic Microwave Background radiation BOOMERanG, CBI, DASI, MAXIMA, ARCHEOPS, WMAP,..... Density components of the Universe

A natural reference : the critical density $\rho_{0,C} = \frac{3H_0^2}{8\pi G} = 1.88 \ h^2 \times 10^{-29} \text{ g/cm}^3 \text{ or } 2.9 \ h^2 \times 10^{11} \text{ M}_{\odot}/\text{Mpc}^3$

 $H_0 =$ Hubble "constant" ($h = H_0/100 \text{ km/s/Mpc} h \approx 0.7$)

 $\Omega = \rho / \rho_C$

Some Ω values [Komatsu et al. 2009]					
Radiation (CMB)	Ω_{R}	5 10 ⁻⁵			
Visible matter	Ω_{L}	≈0.003			
Baryons	Ω_{b}	0.0456±0.0015			
Matter (Dark+Baryonic)	Ω_{m}	0.274±0.013			
Vacuum	Ω_{Λ}	0.726±0.015			
Total	Ω_{T}	≈1.0			

Number of baryons per photon : $\eta = n_b/n_\gamma$ et $\Omega_b h^2 = 3.65 \times 10^7 \eta$

Isotopes to constrain η :

⁴He : little sensitive to η

³He : complex stellar production / destruction history.

D : seems the best candidate: a strong monotonic evolution with η and no stellar production.

 ^{7}Li : main drawback: a non monotonic evolution with η ; two η values for a given Li/H





η×10¹⁰

Anisotropies of the Cosmic Microwave Background (CMB)



(http://map.gsfc.nasa.gov/)



Nucleosynthesis (I)

Equilibrium $p \leftrightarrow n : N_n/N_p = \exp(-Q_{np}/kT); Q_{np} = 1.29 \text{ MeV}$

$$v_e + n \Leftrightarrow e^- + p \qquad \overline{v_e} + p \Leftrightarrow e^+ + n$$

Followed by decoupling and freezeout

Equilibrium as long as the reaction rate is faster than the expansion rate:

$$\Gamma_{\leftrightarrow} >> \frac{\dot{a}(t)}{a(t)} \ (\equiv H(t))$$

Equilibrium breaks out when :

$$\Gamma_{n \leftrightarrow p} \sim G_F^2 T^5 \sim \frac{\dot{a}}{a} = \sqrt{\frac{8\pi G\rho_R}{3}}$$

Then $T \approx 10^{10}$ K and $N_n/N_p \approx 0.2$

$$\rho_{R} = g_{eff}(T) \frac{k^{2} \pi^{2}}{30 \hbar^{3}} T^{4}$$
$$\left(g_{eff}(T) = 4 \Leftrightarrow 11\right)$$

Neutrons decay until *T* is low enough for :

 $n{+}p{\twoheadrightarrow}D{+}\gamma$

becomes faster then deuterium photodisintegration

$$D+\gamma \rightarrow n+p$$
 (Q = -2.2 MeV)

Then, t = 3 mn, $T \approx 10^9 \text{ K}$ and N_n has decrased to $N_n/N_p \approx 0.1$

Nucleosynthesis (II)

Nucleosynthesis starts to produce essentially ⁴He together with traces of D, ³He, ⁷Li,

 $X(^{4}He) \approx 2X(n) \approx 0.2$



Time evolution of baryonic density



 $\rho_b \sim T^3 \; (\sim a^3)$

Negligible influence on expansion rate!

 $\rho_b << \rho_R$

T (K)





In astrophysics:

"metals" = everything beyond helium

Metallicity:

- "metal" mass fraction (*Z*)
- [Fe/H] = $\log(Fe/H) \log(Fe_{\odot}/H_{\odot})$

Solar metallicity

 $Z_{\odot} \approx 0.018$

[Fe/H] **≡**0

Determination of primordial abundances

Primordial abundances :

- 1) Observe a set of primitive objects born when the Universe was young
 - ⁴He in H II (ionized H) regions of blue compact galaxies
 - ³He in H II regions of *our* Galaxy
 - **D** in remote cosmological clouds (i.e. at high redshift) on the line of sight of quasars
 - ⁷Li at the surface of low metallicity stars in the halo of our Galaxy
- 2) Extrapolate to zero metallicity : Fe/H, O/H, Si/H, $\rightarrow 0$

⁴He observations in blue compact galaxies





³He from a sample of 21 local galactic H II regions; upper limit from best observation:

 3 He/H \leq (1.1 \pm 0.2) \times 10⁻⁵ [Bania et al. 2002]



³He primordial abundance ?

New ³He/H data *[Bania et al. 2002]* but at high metallicity : weak constrains on primordial value *[Vangioni-Flam et al. 2002]*.



Deuterium primordial abundance

Fragile isotope : only destroyed after BBN ⇒ use highest observed value

- Local interstellar medium (present) : D/H ≈ 10⁻⁵ [FUSE: Hébrard & Moos 2003, Wood et al. 2004]
- 2. Protosolar cloud (4.6 Gyr ago) : $D/H = (2.5 \pm 0.5) \times 10^{-5}$ [Hersant et al. 2001]
- 3. Remote cosmological clouds on the line of sight of quasars

D/H observations in a cosmological cloud



Cloud at redshift of z = 3.6on the line of sight of quasar QSO 1937-1009 Observations :

•D/H ratio at high redshift from the depth/width of absorption lines

•Baryonic density (Ω_b) from the census of the « Lyman- α Forest » lines





Burles & Tytler 1998a,b; O'Meara et al. 2001; D'Odorico et al. 2001; Pettini & Bowen 2001; Kirkman et al. 2003, Crighton et al. 2004, Pettini et al. 2008

Galactic evolution of Li, Be and B abundances



Observation in halo stars, as a function of « metallicity » ≈ [Fe/H] increasing with time ([Fe/H]=0 : 4.5 Gy ago)

Observation of lithium abundances in low metallicity stars

Spite plateau: Li/H versus metallicity (time): Li/H ≈1.12 10⁻¹⁰ [Spite & Spite, 1982]



•Low dispersion
•⁶Li observations
⇒ In principle, low Li destruction ≈ 0.1 dex (?)
⇒Reliable primordial abundance (?)

 $0.9 \Leftrightarrow 1.9 \times 10^{-10} (2\sigma)$ [Ryan et al. (2000)], $\approx 2.34 \times 10^{-10}$ [Meléndez & Ramírez (2004)] $\approx 1.3 \Leftrightarrow 2.3 \times 10^{-10}$ [Charbonnel & Primas (2005)], $1.1 \Leftrightarrow 1.5 \times 10^{-10}$ [Asplund et al. (2006)]

⁶Li observations in halo stars



The 12 reactions of standard BBN

Origin of reaction rates Theoretical:

• $n \Leftrightarrow p$: with $\tau_n = 885.7 \pm 0.8 \text{ s}$ [PDG 2004] ($\tau_n = 878.5 \pm 0.7 \pm 0.3$ [Serebrov et al. 2005, Mathews, Kajino & Shima 2004]), otherwise small uncertainty [Brown & Sawyer (2001)]

¹H(n,γ)²H : Two nucleons effective field theory [Chen & Savage (1999)]

Experimental :

•New compilation [Descouvemont, Adahchour, Angulo, Coc & Vangioni-Flam (2004)]



≻Cross section :

Cross section (σ) = Number of reactions / time Beam intensity × Number of target nuclei

Thermonuclear reaction rates

 σ units : barn (b) = 10⁻²⁴ cm²

Thermonuclear reaction rate :

$$N_A \langle \sigma \mathbf{v} \rangle = N_A \int_0^\infty \sigma(\mathbf{v}) \mathbf{v} \varphi(\mathbf{v}) d\mathbf{v}$$

φ(v) = Maxwell-Boltzmann distribution

 $N_{\rm A}$ = Avogadro's number

Nuclear network equations



Rate of energy production :

$$\varepsilon = \sum_{ijk} \frac{N_i N_j}{1 + \delta_{ij}} \langle \sigma \mathbf{v} \rangle_{ijk} Q_{ijk}$$



$n \leftrightarrow p$ weak reaction rate

 $\lambda_{n \leftrightarrow p} = \tau_n^{-1} \times$

 $\sum \int (\text{phase space}) \times (\text{e distribution}) \times (\mathbf{v}_{e} \text{ distribution}) \, dE \\ + \text{ small corrections} \\ [Dicus et al. (1982), Brown & Sawyer (2001)] \\ \lambda_{n \rightarrow pev} = C \int_{1}^{q} \frac{\varepsilon(\varepsilon - q)^{2} (\varepsilon^{2} - 1)^{1/2} \, d\varepsilon}{[1 + \exp(-\varepsilon z)] \{1 + \exp[(\varepsilon - q)z_{v}]\}} \xrightarrow{\rightarrow} 0 \quad \frac{1}{\tau_{n}} = C \int_{1}^{q} \varepsilon(\varepsilon - q)^{2} (\varepsilon^{2} - 1)^{1/2} \, d\varepsilon}$

$$(q = Q_{np}/m_e, m_e, \varepsilon = E_e/m_e, z = m_e/T_{\gamma}, z_{\nu} = m_e/T_{\nu})$$

$$\lambda_{n+e^+ \to p+\bar{v}_e}, \quad \lambda_{n+v_e \to p+e^-}, \quad \lambda_{p+e^- \to n+\bar{v}_e}, \quad \lambda_{p+\bar{v}_e \to n+e^+}, \quad \lambda_{p+e^- \to n+v_e} = \dots$$

- $\tau_n = 885.7 \pm 0.8 \text{ s} [PDG 2008]$
- $\tau_n = 878.5 \pm 0.7 \pm 0.3$ [Serebrov et al. 2005]

${}^{1}H(n,\gamma)D$: theory versus experiments

Rate calculated from Effective Field theory with (theoretical) uncertainties of 4% [*Chen & Savage (1999)*] or 1% [*Rupak (2000)*] compared to experiments [*Arenhovel & Sanzone (1991) review*]

BBN energy ~ 25 keV

Additional check with polarized beam *E1* and *M1*measurements [*Tornow et al. (2000)*]

... and new (>1991) cross section measurements [Suzuki et al. (1995), Tomyo et al. (2003)]





Penetrability factor

R_{Class}

E_{Cou}

0

Nucleus

R_{Nucl}

Energy

Coulomb barrier

(+ centrifugal)

Projectile

Distance

► Below the Coulomb barrier!

Coulomb and et centrifugal penetrability :





WKB Approximation : $P_{L=0} \propto \exp(-2\pi\eta)$



Astrophysical *S*-factor:



Gamow energy : $E_G = \frac{1}{2} (2\pi\alpha Z_1 Z_2)^2 \mu c^2 = (0.989 \cdot Z_1 Z_2 A^{1/2})^2 [\text{MeV}]$

 \Rightarrow Much weaker variation of S(E) with energy as compared to $\sigma(E)$

Astrophysical S-factor : S(E)



 \Rightarrow Extrapolation to low energy

10 rates deduced from experimental data

Compilations and evaluations for BBN thermonuclear rates

- Smith, Kawano & Malaney 1999 (with uncertainties)
- > NACRE, Angulo et al. 1999 (7/10, tabulated rates and uncertainties)
- Nollett & Burles 2000 (no rates provided)
- Cyburt, Fields & Olive 2003 (revaluation of NACRE)
- Serpico et al. 2004 (rates and uncertainties provided)
- Descouvement, Adahchour, Angulo, Coc & Vangioni-Flam 2004 [DAACV]
 - « R-Matrix » formalism: S-factors fits of data constrained by theory
 - Provide also reaction rate uncertainties
- > Cyburt 2004 (rates provided, not the uncertainties)







Comparison between observed and calculated abundances

Limits $(1-\sigma)$ obtained by Monte-Carlo from *Descouvemont et al. (2004)* reaction rate uncertainties.

Concordance (?) BBN, spectroscopy and CMB

- Ω_Bh² [WMAP: Spergel et al. (2003,2006)]
- ⁴He [Olive & Skillman (2004)]
- **D** [Fields & Sarkar (2008)]
- ³He [Bania et al. (2002)]

• ⁷Li *[Ryan et al. (1999,2000)]* : difference of a factor of 2-3 between calculated (BBN+CMB) and observed (Spite plateau) primordial lithium



[Coc et al. (2006), Cyburt, Fields & Olive (2008)]

The 12 reactions of standard BBN



Sensitivity to thermonuclear reaction rates

$$\frac{\Delta Y}{Y} = \frac{\partial \ln(Y)}{\partial \ln(N_A \langle \sigma \mathbf{v} \rangle)} \bigg|_{\eta = \eta_{WMAP}}$$

$$\times \frac{\Delta N_A \langle \sigma \mathbf{v} \rangle}{N_A \langle \sigma \mathbf{v} \rangle}$$

At WMAP baryonic density

		$E_0(\Delta E_0/2)$			
Reaction	⁴ He	D	³ He	⁷ Li	(MeV @ 1GK)
τ _n (n⇔p)	0.73	0.42	0.15	0.40	
¹ H(n,γ) ² H	0	-0.20	0.08	1.33	0.025
² H(p,γ) ³ He	0	-0.32	0.37	0.57	0.11(0.11)
² H(d,n) ³ He	0	-0.54	0.21	0.69	0.12(0.12)
² H(d,p) ³ H	0	-0.46	-0.26	0.05	0.12(0.12)
³ H(d,n)⁴He	0	0	-0.01	-0.02	0.13(0.12)
3 H(α , γ) 7 Li	0	0	0	0.03	0.23(0.17)
³ He(n,p) ³ H	0	0.02	-0.17	-0.27	
³ He(d,p) ⁴ He	0	0.01	-0.75	-0.75	0.21(0.15)
³ He(α,γ) ⁷ Be	0	0	0	0.97	0.37(0.21)
⁷ Li(p,α)⁴He	0	0	0	-0.05	0.24(0.17)
⁷ Be(n,p) ⁷ Li	0	0	0	-0.71	

Influence of ${}^{1}H(n,\gamma)D$ reaction rate

(at WMAP/ACDM baryonic density)

 $\Omega_{\rm B} {\rm h}^2 = 0.0224$



 $\Omega_{\rm B} {\rm h}^2 = 0.0224$





E (keV)



Sensitivity = 0.97

 $E_0(\Delta E_0/2) = 0.37(0.21)$ MeV

The ³He(α,γ)⁷Be reaction

Systematic uncertainties : *prompt* versus *activation* measurements

New precise measurements (in particular at LUNA) :

Prompt [Brown et al. 2007, Confortola et al. 2007, Costantini et al. 2008]

 Activation [Nara Singh et al. 2005, Brown et al. 2007, Confortola et al. 2007, Gyürky et al. 2007]
 Recoil [Di Leva et al. 2009]

Reanalysis of ³He(α,γ)⁷Be rate [*Cyburt* & *Davids 2008*]: *S*(*0*) = 0.580±0.043 keV.b (13% higher than in DAACV04)











Excellent agreement with *DAACV* 2004 fit within Gamow window

- ≻ No change in central Li/H value
- Reduced uncertainty
- ≻ R-matrix fit reliability



Astrophysical aspects

Extracting Li/H abundances from observed atomic spectra (See Ryan et al. 2000)

- Extrapolation to zero metallicity
- > 1D versus 3D atmosphere model
- Surface gravity
- Non Local Thermodynamical Equillibrium
- Stellar depletion [Richard, Michau & Richer, 2005; Korn et al. 2006]
 - Diffusion and turbulent mixing depletes Li surface abundance
- Effective temperature scale [Hosford et al. 2008]
 - Improved temperature scale ($\Delta Li/Li \approx 6 \ 10^{-4} \ \Delta T_{eff}$) : Li/H = (1.14±0.07)×10⁻¹⁰ (reduced uncertainty)

The Li problem update

New ³He(α , γ)⁷Be and n(p,g)d rates :

- Li/H = (5.24±0.67)×10⁻¹⁰ [Cyburt, Fields & Olive 2008]
- Li/H = (5.14±0.50) ×10⁻¹⁰ [Coc & Vangioni 2010]

New abundance determinations :

Li/H = (1.14±0.07)×10⁻¹⁰ [Hosford et al. 2008],
□⁷Li difference of a factor of ≈5 rather than ≈3!





	BBN calculations		Observations	
	Cyburt et al. 2008	Coc & Vangioni 2010		
⁴He	0.2486±0.0002	0.2476±0.0004	0.232-0.258	×10 ⁰
D/H	2.49±0.17	2.68±0.15	2.84±0.26	×10 ⁻⁵
³ He/H	1.00±0.07	1.05±0.04	(0.9-1.3)	×10 ⁻⁵
⁷ Li/H	5.24 ^{+0.71} -0.62	5.14±0.50	1.14±0.07	×10 ⁻¹⁰

Other nuclear reaction rates

- •About 100 other reactions involved in SBBN from H to B
- •Among them ≈40 remain whose uncertainty on rate is not available
- Systematic check by varying the rates by factors of 10, 100, 1000.

An interesting case : the $^7Be(d,p)2\alpha$ reaction



Experimental data on $^7Be(d,p)2\alpha$ reaction

Reaction rate [CF88] from an estimate [Parker, 1972] based on partial experimental data [Kavanagh, 1960]

No data at BBN energies! Only 8Be g.s. and 1st level





The ⁷Be(d,p) 2α experiment

Centre de Recherche du Cyclotron, Louvain-la-Neuve







Beam : 0.2-1. 10⁷ pps of ⁷Be at 5.8 MeV, degraded to 1.8 MeV (0.4 MeV c.m.) Target : 200 μ g/cm² CD₂ poliethylene Detectors : two (LEDA) multistrips (8× 16) Si detectors (300 and 500 μ m)

Integrated ($\Delta E \approx 0.23$ MeV) cross section [Angulo et al., ApJL (2005)]

 $^{7}Be(d,p)2\alpha$ cross-section



⁹B ground state and first excited level contribution (comparison with Kavanagh)
 ^{All} ⁹B level contribution
 ^{No cross section enhancement}

A new resonance in ⁷Be(d,p) 2α ???

□Hypothetical resonance at $E_R = 200 \pm 100$ keV with $\Gamma \leq 40$ keV [Cyburt & Pospelov 2009]

≻ corresponding to a ⁹B level analog of the 16.7 MeV 5/2+ one in ⁹Be

 \succ extreme Γ_d value at "Wigner limit" with very large interaction radius

> within limits given by Louvain-la-Neuve experiment



⁶Li nucleosynthesis

At WMAP baryonic density



12 main reactions for ⁴He, D, ³He, ⁷Li (+2 for ⁶Li) nucleosynthesis: 10 (+2) from experiments and 2 from theory

The ⁶Li problem vs nuclear physics



The ${}^{2}H(\alpha,\gamma){}^{6}Li$ rate in NACRE



E (MeV)

2 H(α , γ)⁶Li \Leftrightarrow ⁶Li Coulomb dissociation



Coulomb dissociation of ⁶Li





Coulomb dissociation of ⁶Li at GSI

□ From *S. Typel*'s calculations :

> At 150 A MeV (GSI), the nuclear breack-up contribution is important

> At 26 A MeV [Kiener al. 1991], the nuclear breack-up contribution is dominant



[Hammache et al. 2010]



[Hammache et al. 2011]

Isotopes produced during BBN

Absence of stable A=5 and 8 nuclei limits nucleosynthesis





-21 10

10 -22

1

2

3

Beryllium and Boron are not produced in observable quantities during (standard) BBN.

 η_{10}

9 10

8



Origin of CMB, SBBN and Li observations discrepancies

□ Nuclear physics : *Most probably no* but important!

 \succ To quantify the amount of needed depletion

Stellar depletion : Possibly ?

Persistence of a plateau ? ⁶Li ?

□ Standard BBN inadequate :?

Modified gravity

Variation of fundamental constants

Catalysis by charged heavy relics

➢ Heavy particle decay

▶

□ When looking back in time, *Standard* BBN is the last milestone of know physics