

**STUDIES ON SOME QUANTUM
INTEGRABLE SPIN CHAINS WITH
LONG-RANGE INTERACTION**

**THESIS SUBMITTED TO
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By

**NILANJAN BONDYOPADHAYA
SAHA INSTITUTE OF NUCLEAR PHYSICS
KOLKATA**

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