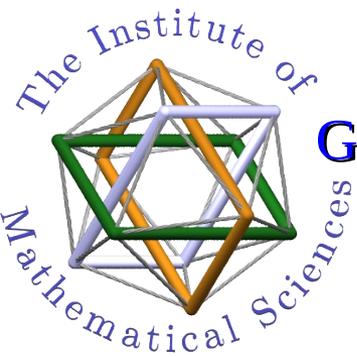


Colorful Nuclei and *Condensed Matter*

Prof M K Pal 2nd Memorial Lecture

March 29, 2019



G Baskaran

Chennai



PERIMETER INSTITUTE
FOR THEORETICAL PHYSICS

Waterloo, Canada





Professor Mamoj Kumar Pal

1932-2016

Distinguished Theoretical Nuclear Physicist

Former Director of SINP

Great Teacher

**School of Nuclear Physics established by
M K Pal and M K Banerjee**

**Co Director of Schools and Workshops in Nuclear Physics
at the International Center for Theoretical Physics, Trieste, Italy
for 16 years**

Books by Prof M K Pal

Theory of Nuclear Structure

Special Theory of Relativity

General Theory of Relativity

Forever Free (Historical Novel)

**Old Wisdom and New Horizon
(on Science, Religion and Philosophy)**

Cosmology (unfinished)

**Friends and colleagues describe him as
Multifaceted genius ... highly spiritual person**



ICTP



**I am fortunate to have met Prof M K Pal
during 1976 – 1984 at ICTP**

Acknowledgement

Discussions with Colleagues at Matscience

***M.V.N. Murty, Sayanthan Sharma, Mukul Laad,
G Rajasekaran, Rahul Sinha ...***

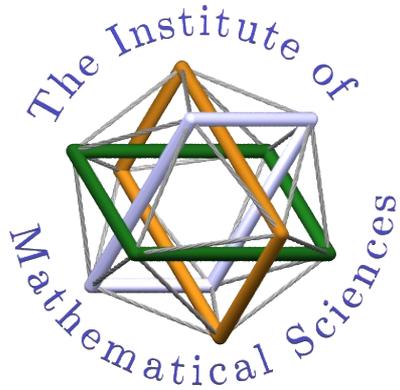
Supported By

SERB, DST, India

Perimeter Institute for Theoretical Physics, Canada

About my Institute

<http://www.imsc.res.in>



Institute of Mathematical Sciences

Research in

Theoretical Physics
Pure Mathematics
Computer Science

~ 60 faculty
100 Ph.D. students
20 PDF's
10 visitors

Junior Research Fellow

Entrance through **JEST** Exam

Autonomous Institute

Post Doctoral Fellowship

Visiting Research Scholar

Summer Program for BSc, BE, MSc students

Faculty Associateship

Adjunct Faculty

Visiting Professor...

similar to

IIT's

IISc, Bangalore

SINP, Kolkata

TIFR, Bombay

DAE Aided Institute



Stephen Hawking Center

**PI PERIMETER
INSTITUTE**
Waterloo, Ontario, Canada

www.perimeterinstitute.ca

Research Institute similar to Matscience
but extensive visitor program



Perimeter Scholars International (PSI) Program (hosts a wealth of Videos of Lecture Courses)

An example of respect by an individual for theoretical physics
as something that helps transform society (**Maxwell Equations**)

**other examples – Kavli, Yuri Millner, Simons
Mahendra Lal Sarkar, Tata, Alagappa, Birla, Mehta, Annamalai,
Azhagappa, A C Muthiah, K B Chandrasekaran ... Krish Gopalakrishnan ..
Azim Premji, Narayanamurthy, Shiv Nadar, ...**



Mike Lazaridis

**Donor of
~ 400 Million \$
(Black Berry Chief)**

Private Funding for Basic Science in india ?

Science Philanthropy Alliance (USA)

Boldness of the Philanthropists – David Baltimore (Science Magazine)

Usefulness of Useless Science

There is a long tradition of exchange of ideas between nuclear physics and quantum condensed matter physics.

Eugene Wigner Nobel Prize for Nuclear Physics



1902-1995

**An early bridge between
Nuclear and Solid State Physics**

**Wigner Eckart Theorem, Wigners 3-j symbol
Symmetry principle in nuclear physics
Random matrix theory of nuclear spectra
Crystalline Correlation inside Nuclei
Jordan-Wigner transformation**

**Wigner-Seitz cell, Wigner (electron) crystal
Wigner-Huntington (metallization of solid hydrogen
Route to Room Temperature Superconductivity ?**

**John Bardeen, Ph.D. student of Wigner won 2 Nobel Prizes
Discovery of Transistor and BCS Theory of Superconductivity**

Traditionally we discuss nucleus of atoms using shell model, as atomic mass increases. Filling of shells is well known for electrons in atoms, where positively charged nucleus bind together mutually repelling electrons.

In a nucleus there is no attracting center. Protons and neutrons hold themselves together using strong-mutual nuclear forces. Physics beyond shell model has been suggested ... (liquid droplry model, alpha clustering ...)

That is, certain nuclei may support novel quantum novel many body states.

Quantum crowd of electrons in some crystalline solids or liquid He4 droplets could help understand this.

Attraction between two nucleons via exchange of Meson (Yukawa)

Phonon mediated attraction between two electrons in a metal (Frohlich)

and BCS theory of pairing superconductivity

**Pairing in Nuclei - Superfluidity in Neutron Stars
Vortex lattice, pinning, neutron star quakes, ...**

Color Superconductivity, Quark Gluon Plasma

Alpha particle Clustering ...

Linear chain of alpha particles !

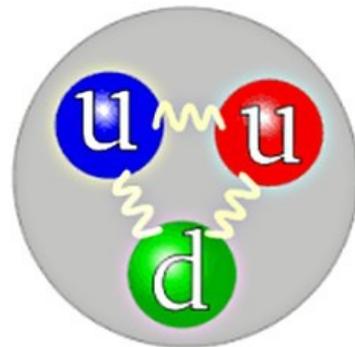
Bose Condensation ... Quantized Vortices in rotating Nuclei

Skyrmion Model of Nucleon

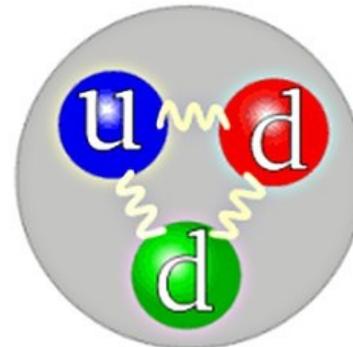
(Baby) Skyrmion Crystals in Magnets (MnSi)

In a nucleus, colorful quarks and gluons are confined by strong QCD forces, It results in integer electric charges and color singlet states.

Is it possible to get a transient glimpse of color of gluons and quarks or fractional charges of quarks, in some low energy nuclear physics experiments, without use of high energy collider machines ?



Proton



Neutron

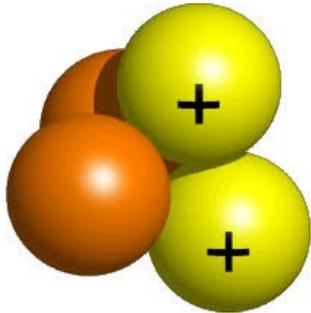
Quark composition of a proton and a neutron (diagrams from *Wikipedia*)

Alpha clusters in Nuclei

Molecules of alpha particles ... Bose Condensation

Alpha – chain (statistics transmutation ?)

2 protons and 2 neutrons



Bound State of 2 Deutrons ?

Deuteron is an Isospin Singlet & Spin Triplet

Nature of the singlet

Spin = 0

Charge = + 2e a Boson

Alpha clusters in Light Nuclei

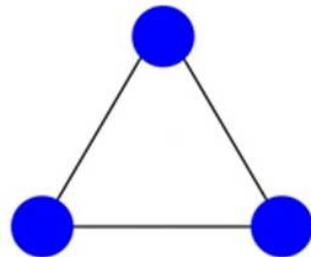
Molecules of alpha particles



${}^8\text{Be}$

Dumbbell

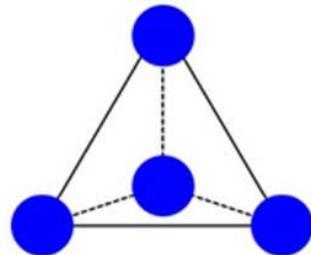
Z_2



${}^{12}\text{C}$

Triangle

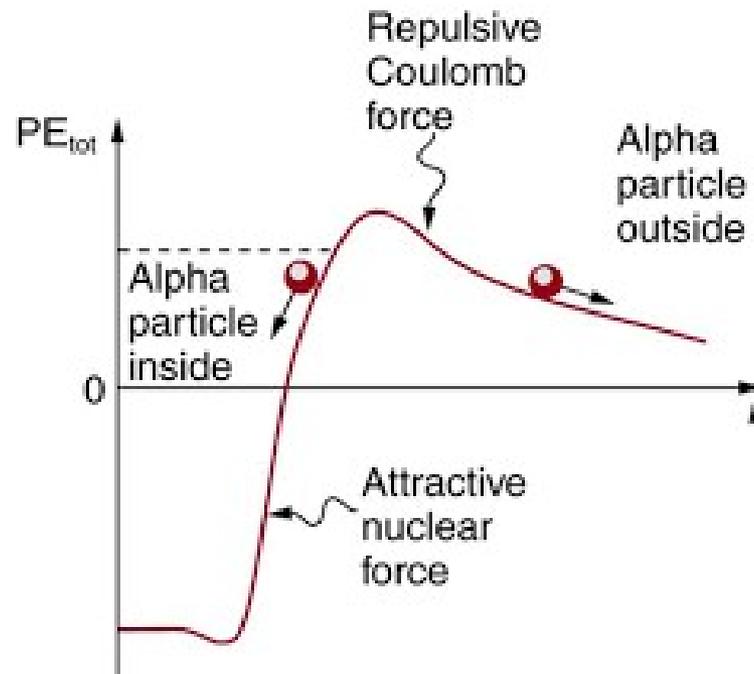
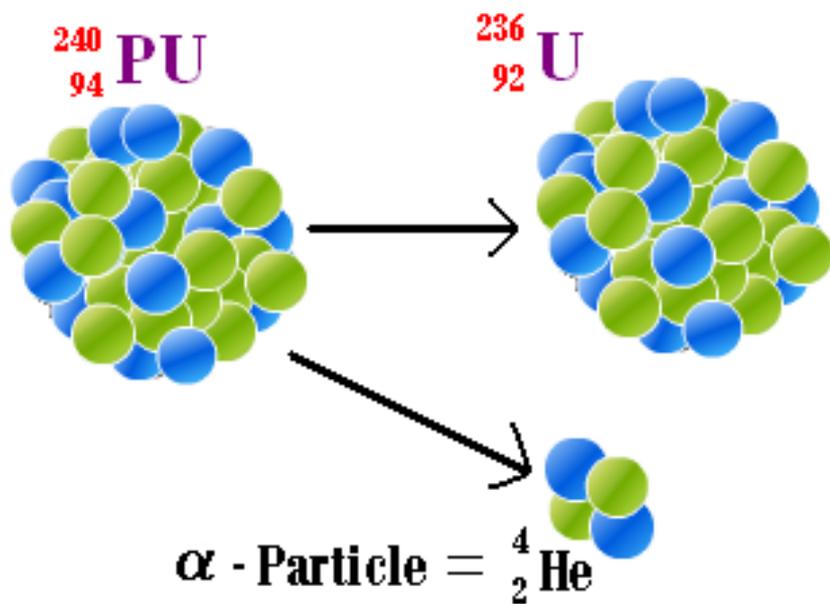
D_{3h}



${}^{16}\text{O}$

Tetrahedron

T_d



Alpha clusters in Nuclei

Molecules of alpha particles Bose Condensation

Deuteron is an Isospin Singlet & Spin Triplet

P N P N P N P ...

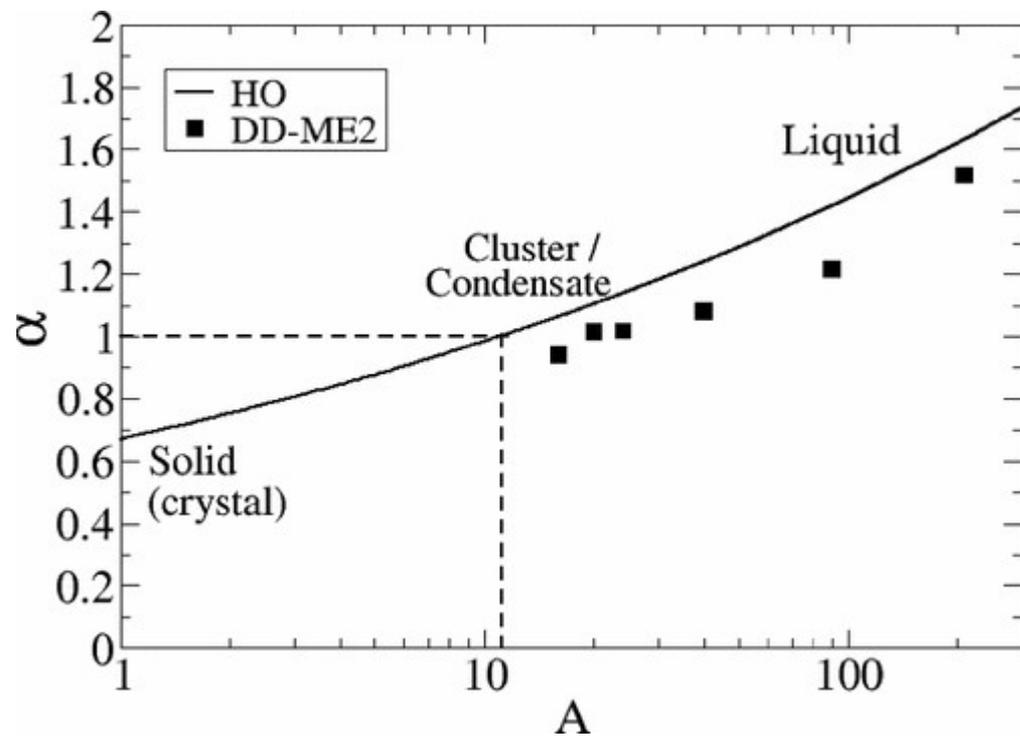
Isospin Heisenberg AFM Chain ?

Rotating nuclei ?

Resonating Valence Bond State ?

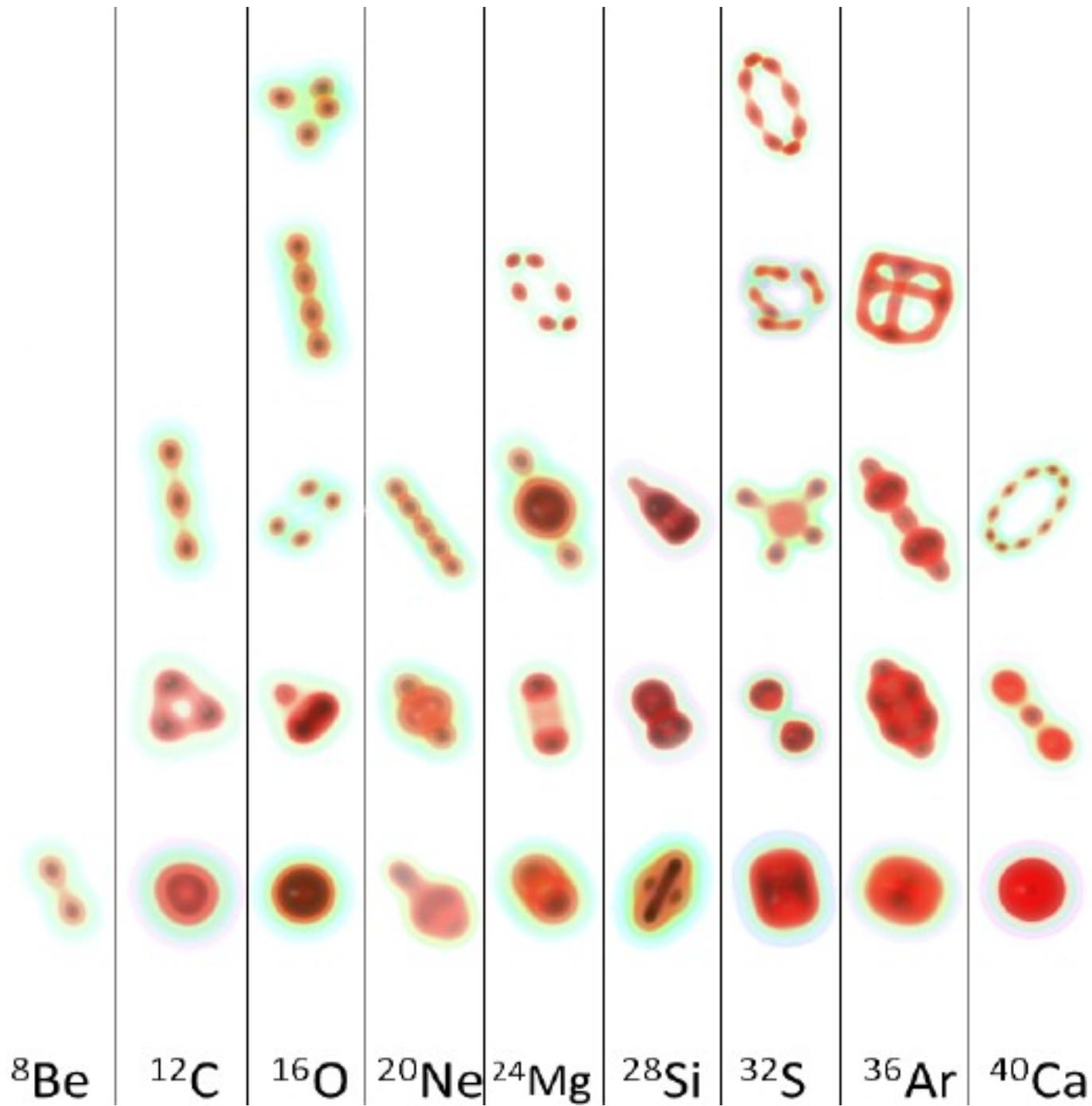
IsoSpinon Excitation - Isospin half charge $e/2$?

(GB 2019)



Density Functional Theory studies of cluster states in nuclei

J.-P. Ebran,¹ E. Khan,² T. Nikšić,³ and D. Vretenar³

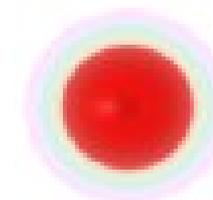
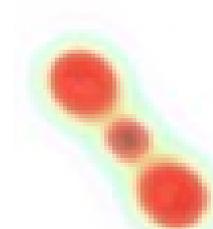


Consider Calcium nucleus

Alpha particles are hard core bosons

Jordan-Wigner Transformation

Alpha particles in the Chain behaves like Fermions !



^{40}Ca

Is heavy nucleus like Plutonium or Uranium a Superfluid of alpha particles ?

Lattice Nuclear Physics

Ulf-G. Meißner, Univ. Bonn & FZ Jülich

Quantum phase transition from Bose gas of α 's to nuclear liquid for α -type nuclei

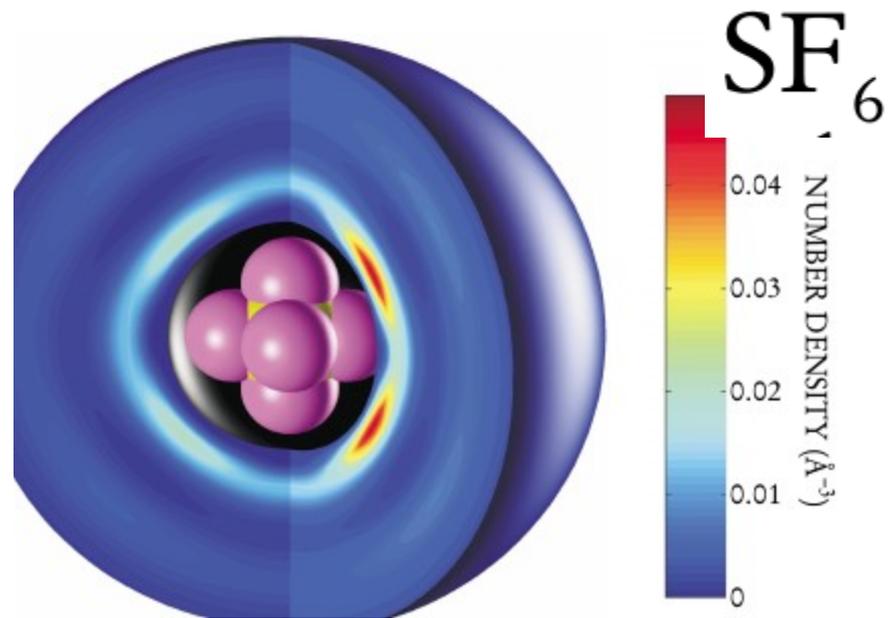
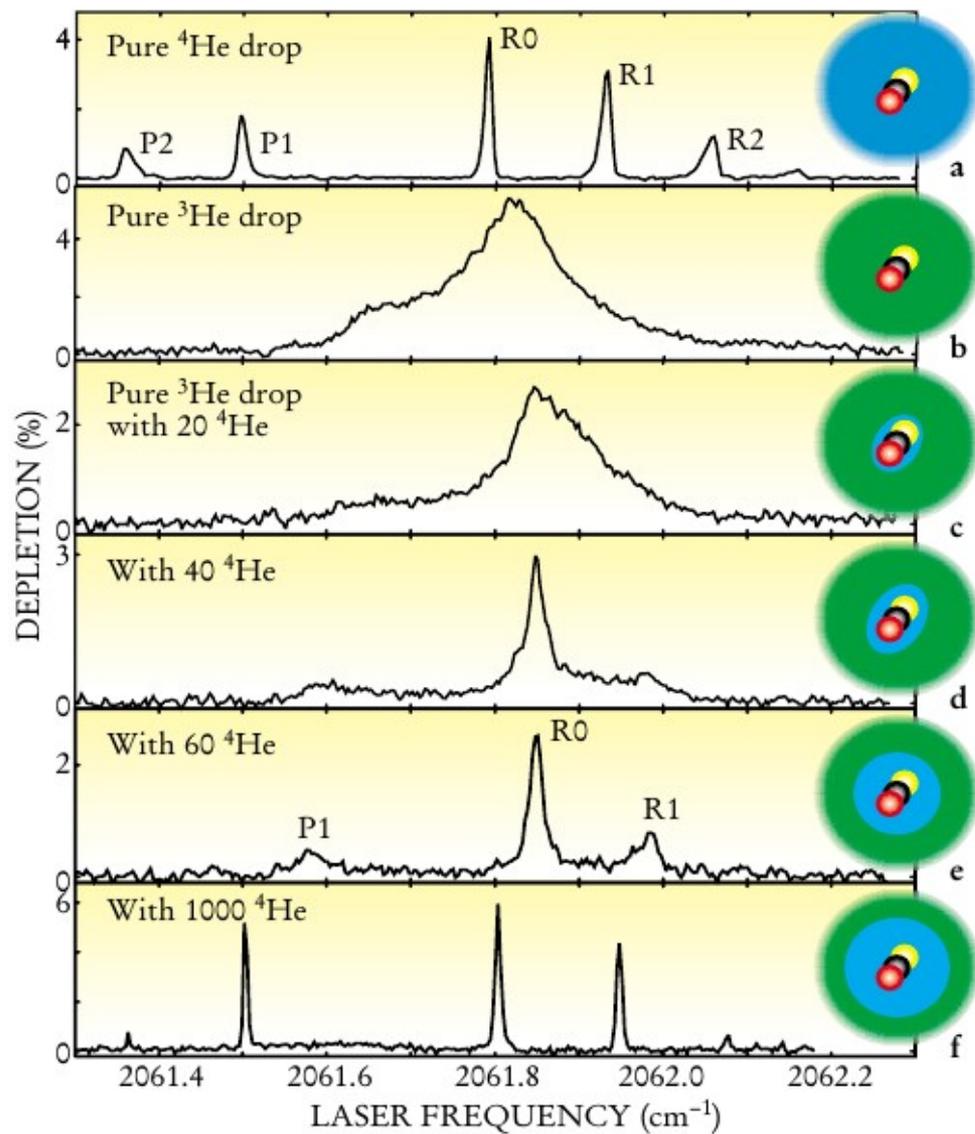
Experiments (Gotingen)

**A droplet of He4 atoms becomes a superfluid
When number of He4 atoms exceeds 60 !**

Superfluid Helium Droplets: An Ultracold Nanolaboratory

J. Peter Toennies, Andrej F. Vilesov, and K. Birgitta Whaley

Physics Today **54**, 2, 31 (2001)



COS
molecule

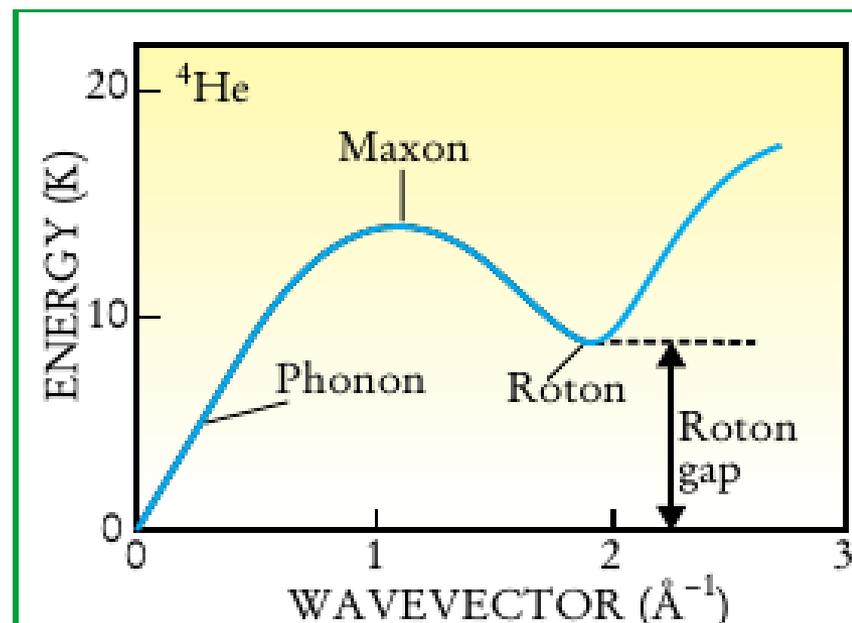
Direct Spectroscopic Observation of Elementary Excitations in Superfluid He Droplets

M. Hartmann, F. Mielke, J. P. Toennies, and A. F. Vilesov

Max-Planck-Institut für Strömungsforschung, Bunsenstrasse 10, D-37073 Göttingen, Germany

G. Benedek

Istituto Nazionale di Fisica della Materia, Dipartimento di Fisica dell'Università, via Celoria, I-20133 Milano, Italy



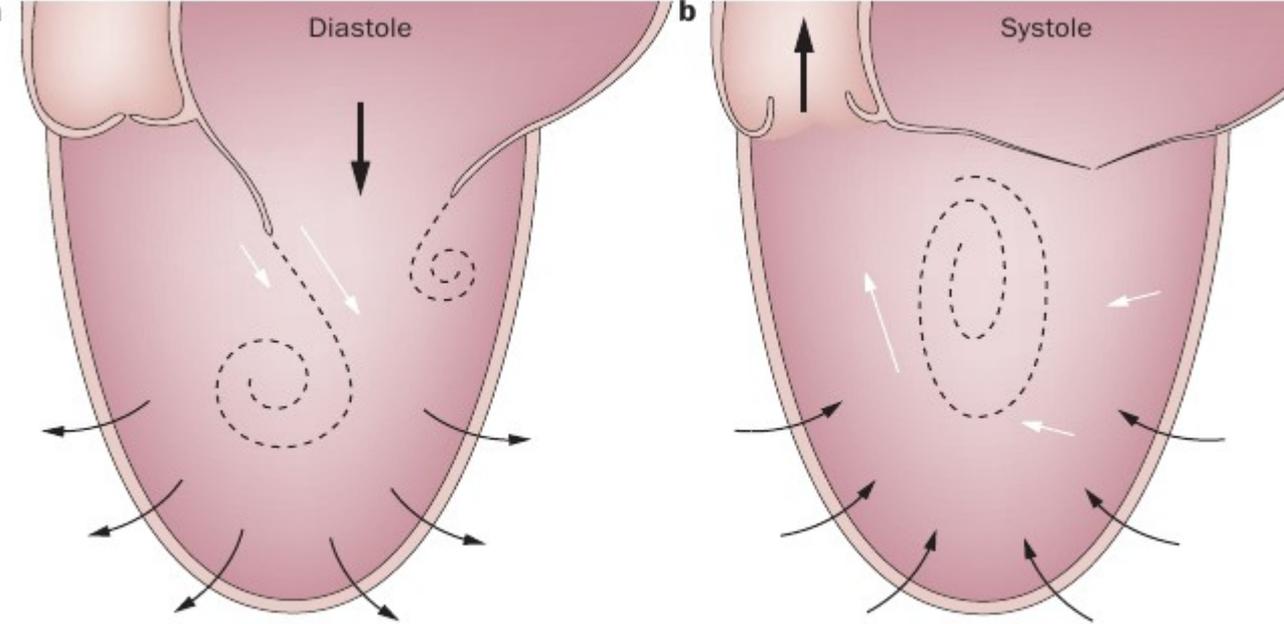
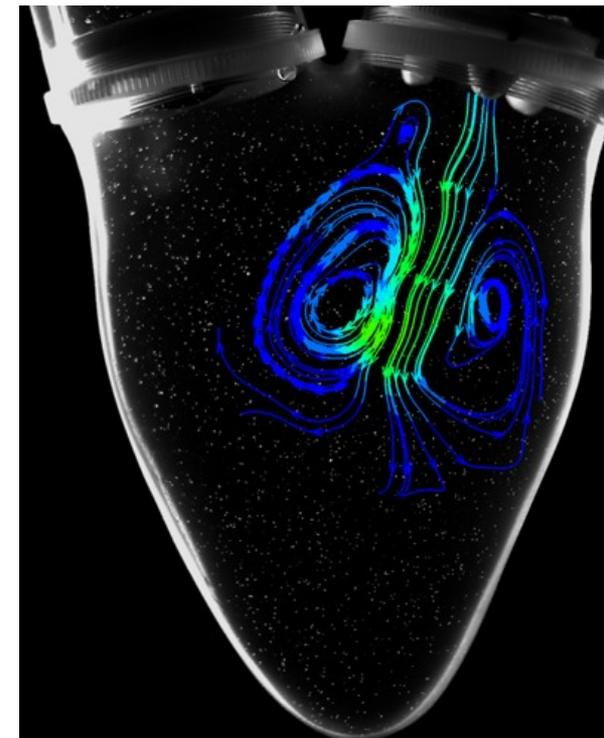


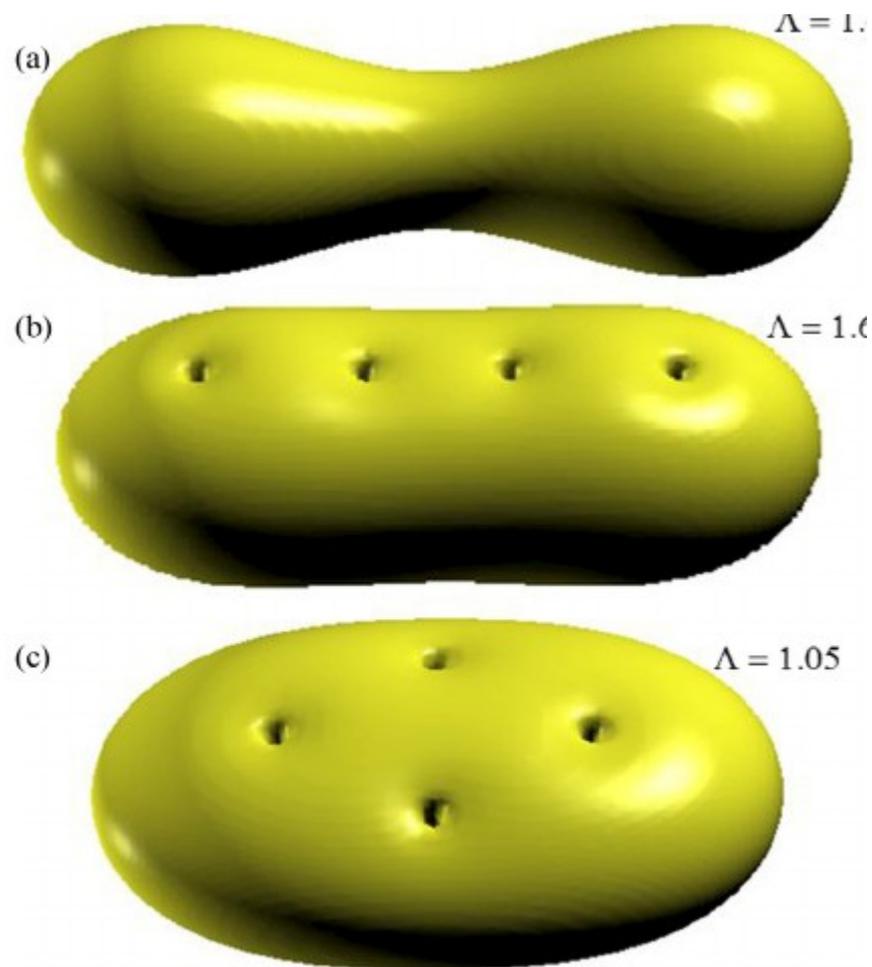
Figure 1 | Blood flow in the healthy left ventricle. **a** | Blood flows into the left ventricle during diastole (thick black arrow), propelled by base-to-apex pressure gradients (thin black arrows).

The vortex—an early predictor of cardiovascular outcome?

Gianni Pedrizzetti, Giovanni La Canna, Ottavio Alfieri and Giovanni Tonti



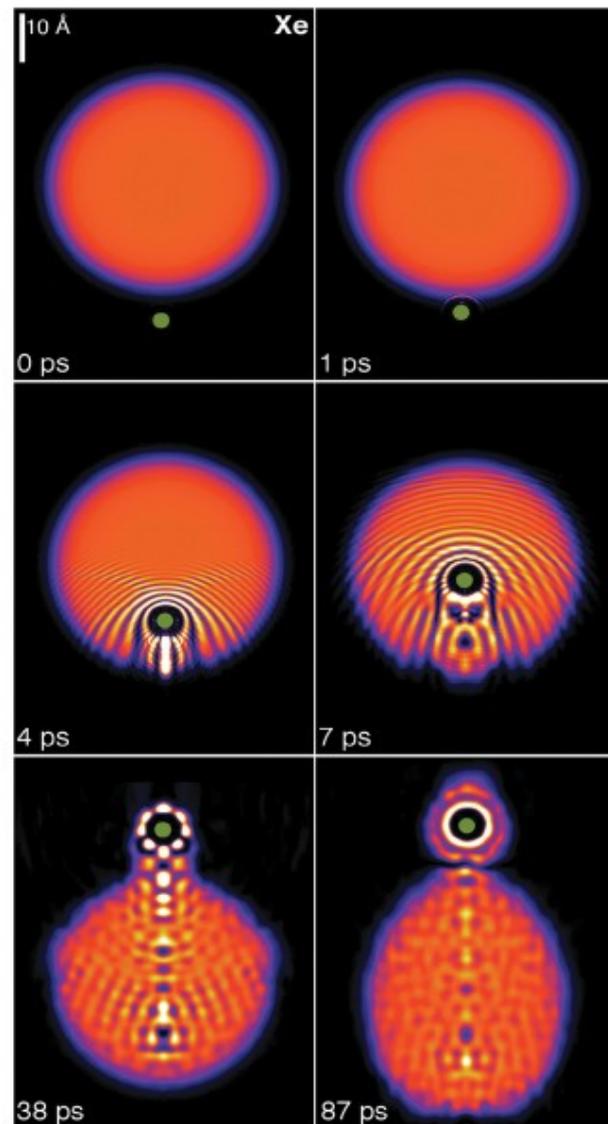
Spinning superfluid ^4He nanodroplets



Capture of Xe and Ar atoms by quantized vortices in ^4He nanodroplets†

François Coppens,^{id}*^{ab} Francesco Ancilotto,^{cd} Manuel Barranco,^{abef}
Nadine Halberstadt^{ab} and Martí Pi^{ef}

Phys. Chem. Chem. Phys., 2017, **19**, 24805–24818

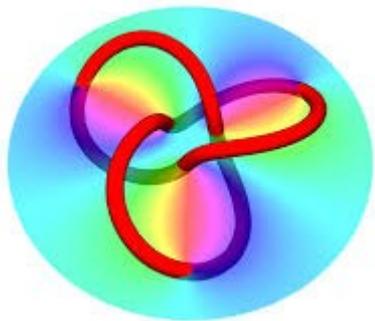
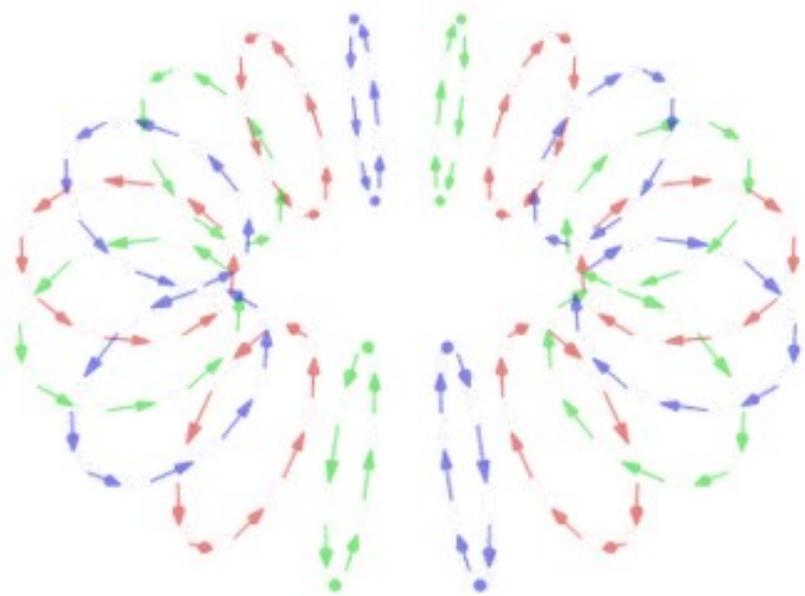


Is heavy nucleus like Plutonium or Uranium a Superfluid of alpha particles ?

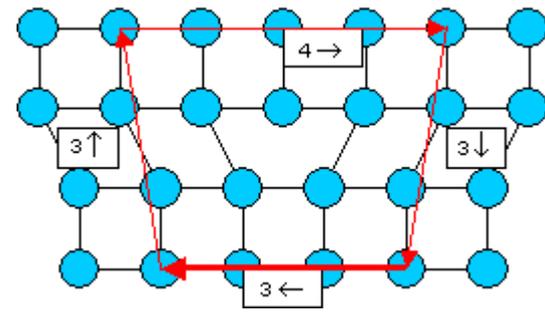
Do we produce quantized vortices in rotating Nuclei ?

**Anomalous stability of some Isomers - Tangled Vortices ?
Vortex Knots ?**

GB 2019



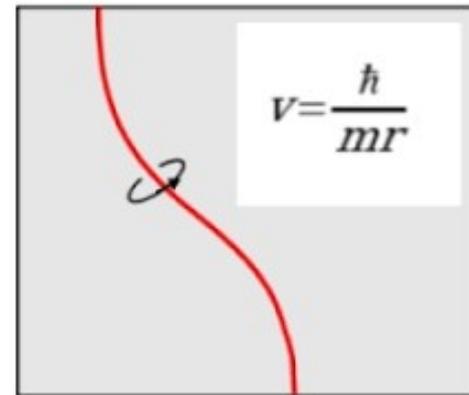
Dislocation - Burgers vector



Quantized Vortices in superconductors, superfluids

Topological Soliton - Skyrmion in Nuclear Physics

Baby Skyrmion in Magnets



A quantized vortex

Skyrmion Crystals

Spintronics

Chiral symmetry breaking and Pion condensation

Skyrme model of nucleon

Topologically non trivial configuration of pion condensate

Topological Defects condensed matter He3, ...

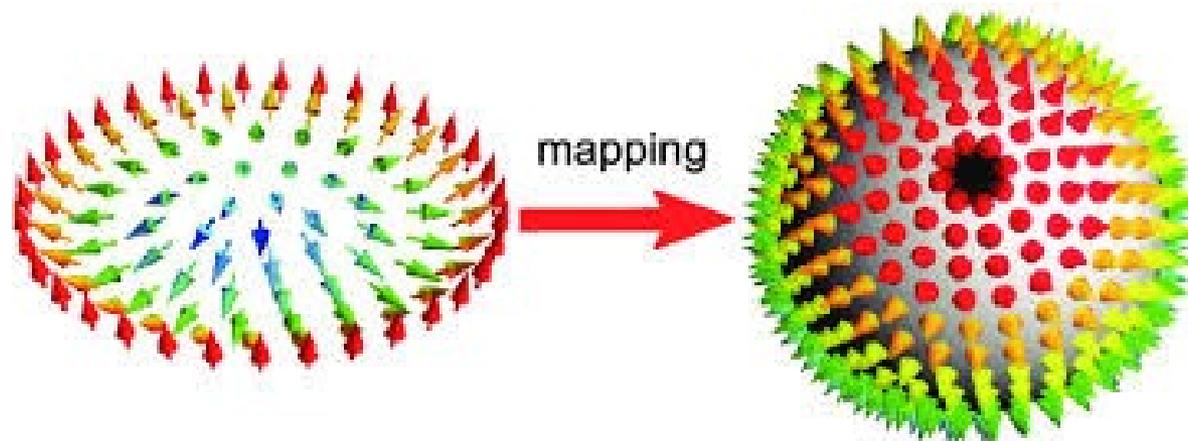
Homotopy Theory

Skyrmion in ferromagnets and antiferromagnets, Hopf term, ...

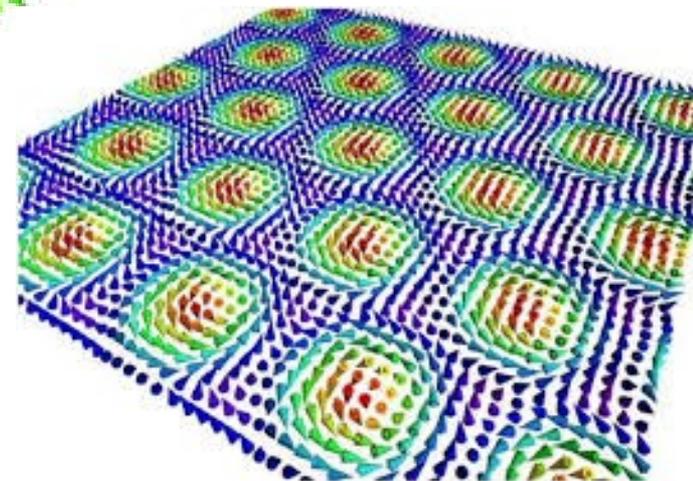
Skyrmion as a two spinon state (GB 2001)

Skyrmion crystals in Magnetic Materials

Spintronics



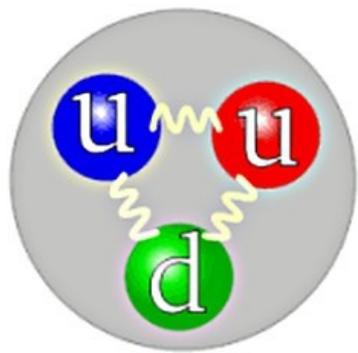
$$n = \frac{1}{4\pi} \int \mathbf{M} \cdot \left(\frac{\partial \mathbf{M}}{\partial x} \times \frac{\partial \mathbf{M}}{\partial y} \right) dx dy$$



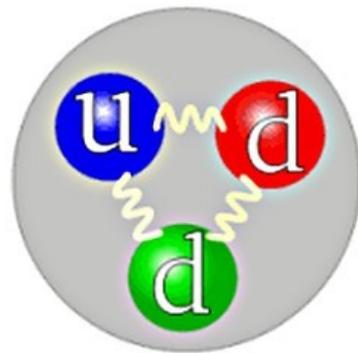
Three Generations
of Matter (Fermions)

	I	II	III	
mass →	2.4 MeV/c ²	1.27 GeV/c ²	171.2 GeV/c ²	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin →	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name →	u up	c charm	t top	γ photon
	4.8 MeV/c ²	104 MeV/c ²	4.2 GeV/c ²	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
Quarks	d down	s strange	b bottom	g gluon
	<2.2 eV/c ²	<0.17 MeV/c ²	<15.5 MeV/c ²	91.2 GeV/c ²
	0	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z⁰ Z boson
	0.511 MeV/c ²	105.7 MeV/c ²	1.777 GeV/c ²	80.4 GeV/c ²
	-1	-1	-1	±1
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
Leptons	e electron	μ muon	τ tau	W[±] W boson
				Gauge Bosons

Can we get a glimpse of colors and fractional charges in
Some low energy nuclear physics experiments ?



Proton



Neutron

Quark composition of a proton and a neutron (diagrams from *Wikipedia*)

